

# Supplemental Document: Self-Calibrating, Fully Differentiable NLOS Inverse Rendering

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This supplemental document provides additional information and results in support of the primary document. Refer to Table 1 for the notations and symbols used in this paper.

## 1 JOINT LASER-SENSOR CORRELATION MODEL

The joint laser-sensor model is derived as Equation 1 following the previous related work [Chen et al. 2020; Hernandez et al. 2017].

$$\begin{aligned} \mathbf{H}_R &= P_{PDE} \cdot (\Phi * (\Lambda * \mathbf{H}_r + L_a)) + L_{DCR} \\ &= (\Phi * \Lambda * \mathbf{H}_r + \Phi * L_a) + L_{DCR} \\ &= ((E_s * G_s) * G_l * \mathbf{H}_r + (E_s * G_s) * L_a) + L_{DCR} \\ &= ((E_s * (G_s * G_l) * \mathbf{H}_r + (E_s * G_s) * L_a) + L_{DCR}), \quad (1) \\ &= (E_s * G_{I_s} * \mathbf{H}_r + (E_s * G_s) * L_a) + L_{DCR} \\ &= (\Psi(t; I_l, \kappa_s, \sigma_{I_s}) * \mathbf{H}_r + L_a) + L_{DCR} \\ &= \Psi(t; I_l, \kappa_s, \sigma_{I_s}) * \mathbf{H}_r + \eta_s \end{aligned}$$

where  $P_{PDE}$  denotes the photon detection efficiency.  $L_a$  is the ambient light and  $L_{DCR}$  is the dark count rate.  $\Phi$  is the sensor model function that can be expressed in the form of convolution between exponential function  $E_s$  and Gaussian function  $G_s$ .  $\Lambda$  is the laser function that has the shape of Gaussian  $G_l$ . Note that the convolution of two Gaussians  $G_s$  and  $G_l$  can be merged to a single Gaussian  $G_{I_s}$ . The convolution of  $E_s$  and  $G_{I_s}$  is then expressed as  $\Psi$  that has three parameters  $I_l$ ,  $\kappa_s$ , and  $\sigma_{I_s}$ .  $L_a$  and  $L_{DCR}$  can be summed to a single offset value  $\eta_s$ . Our joint laser-sensor correlation model finally has four parameters and these values are optimized in our self-calibrating pipeline.

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## 2 EXPERIMENTAL DETAILS

Table 2 summarizes the type of data (confocal or non-confocal), as well as the dimensions of the transient data, the dimensions of the reconstructed volume, the total reconstruction time, and the number of iterations before convergence; note that most of our scenes are significantly larger than previously reported results by transient optimization methods.

## 3 ADDITIONAL RESULTS

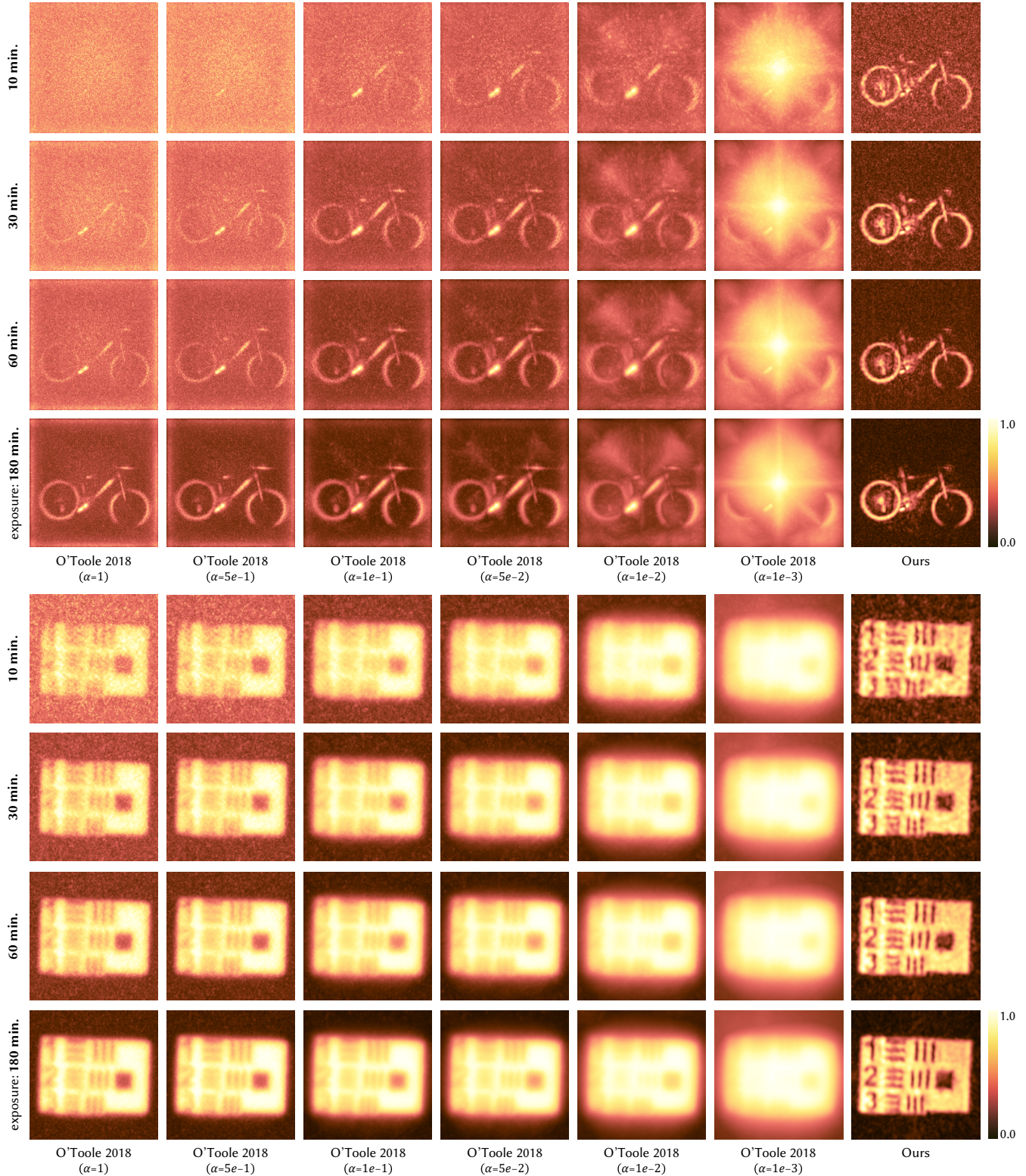
This section provides additional validations and results.

*Manual parameter adjustment vs. our self-calibration.* Figure 1 compares the estimated volumetric intensities of BIKE and RESOLUTION scenes by two different methods: the light cone transform (LCT) [O’Toole et al. 2018] and ours. To handle noise in the input dataset, we manually tweak the SNR parameter in the LCT method with a very wide range from 0.001 to 1.0. Our method yields clearer results than any of the results under the explored values for the SNR parameter of LCT, throughout all exposure levels.

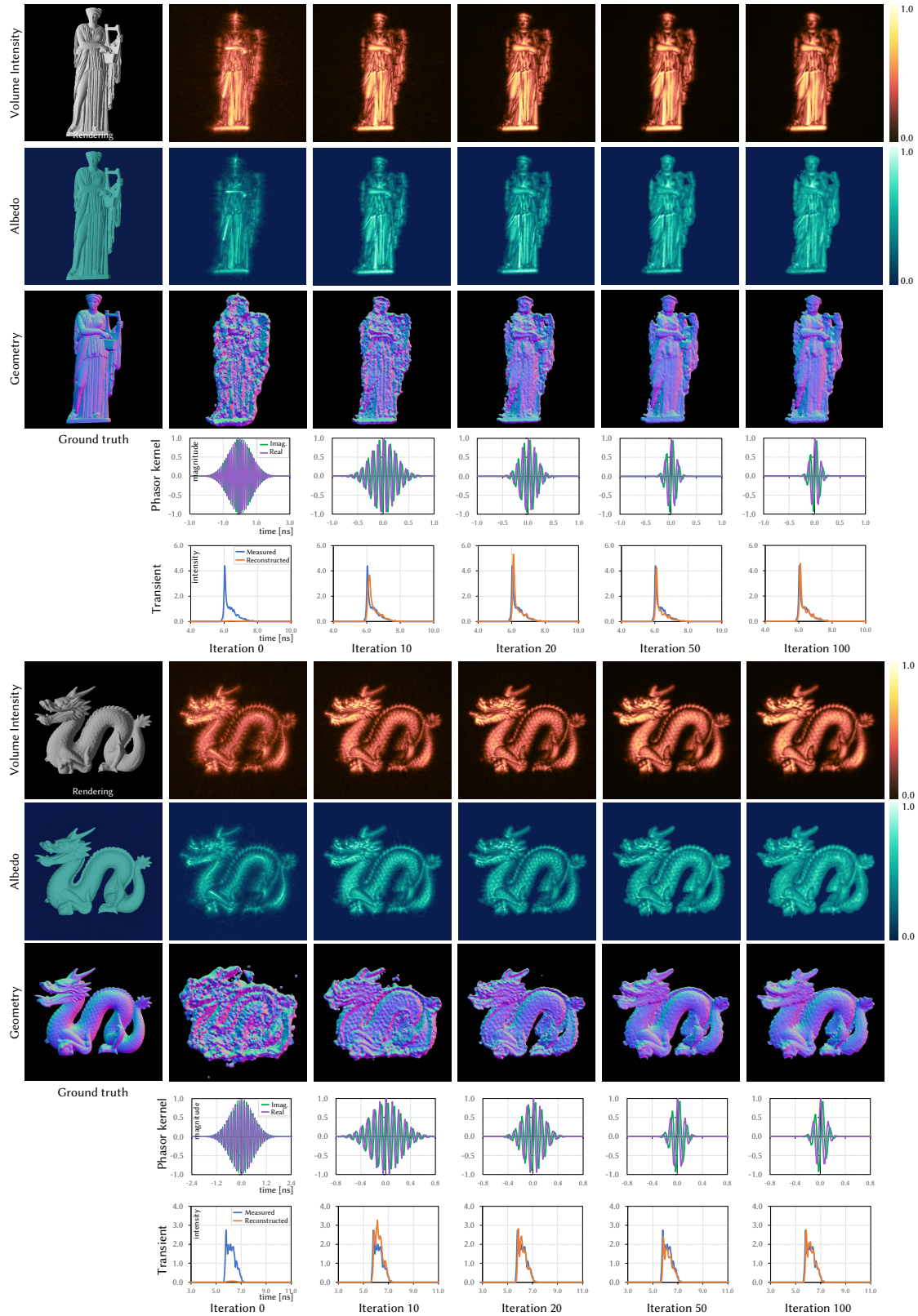
*Progressive optimization results.* Figure 2 show detailed progress of the optimization in the DRAGON and ERATO scenes, displaying the evolution of the phasor-field kernel until the converged state. While the full optimization takes 100 iterations (1.28 hours), after only 50 iterations (39 minutes) the converged phasor-field kernel parameters already yield volumetric and geometric reconstructions very close to the converged result, while the remaining iterations refine more local details.

## REFERENCES

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**Figure 1: Comparisons of the estimated volumetric intensities of BIKE and RESOLUTION scenes by the light cone transform [O'Toole et al. 2018] and ours. To handle noise, we changed the SNR parameter  $\alpha$  between 1 and 0.001 for different exposure times. In all exposure levels, our volume intensities outperform those of the LCT with manually selected parameters.**



**Figure 2: Progressive optimization of volumetric intensity, geometry, phasor kernel, and transient measurement samples of the ERATO and DRAGON scenes, showing how our reconstructions quickly converge after only 100 iterations.**

**Table 1: Main notations and symbols used in the paper.**

Symbol	Description
$\bar{\mathbf{x}} = \mathbf{x}_0 \dots \mathbf{x}_k$	Light path of $k + 1$ vertices
$\mathbf{x}_l$	Light source point on the relay wall
$\mathbf{x}_g$	Surface point in the hidden scene
$\mathbf{x}_s$	Sensor point on the relay wall
$\mathbf{x}_v$	Voxel in a volumetric grid
$\mathbf{n}_g$	Surface normal in the hidden scene
$G$	Scene geometry parameters: points $\mathbf{x}_g$ and normals $\mathbf{n}_g$
$\mathbf{t} = t_0 \dots t_k$	Time delays on $k + 1$ vertices
$d$	Distance between the hidden surface and the relay wall
$\psi$	Space of all light paths
$\psi_k$	Space of light paths of $k + 1$ vertices
$\mathcal{T}$	Space of temporal delays
$c$	Speed of light in vacuum
$\text{tof}(\bar{\mathbf{x}})$	Total time of path $\bar{\mathbf{x}}$
$\mathcal{K}$	Time-resolved path contribution
$H$	Transient measurements
$H_{pf}$	Transient measurements filtered by a phasor kernel
$H_r$	Rendered transient illumination
$H_R$	Rendered transient after laser-sensor model applied
$D(\cdot)$	Geometry estimation function
$\rho(\cdot)$	Reflectance function at vertex
$V(\cdot)$	Visibility function
$\mathfrak{Z}(\cdot)$	Path throughput with geometric attenuation/visibility
$R(\cdot)$	Transient rendering function
$I_{pf}$	Volumetric intensity backprojected by Rayleigh-Sommerfeld integrals of phasor-field diffraction
$\Omega_{pf}$	Illumination frequency of phasor field kernel
$\sigma_{pf}$	Illumination standard deviation of phasor field kernel
$\mathcal{P}(\cdot)$	Filtering function with a phasor field kernel
$I_l$	Laser energy intensity
$\sigma_l$	Standard deviation of Gaussian laser pulse signal
$\kappa_s$	Sensor sensitivity decay rate
$\eta_s$	Sum of ambient light and sensor dark count rate
$\sigma_{I_s}$	Standard deviation of Gaussian parameter for $\Psi(\cdot)$
$\Lambda(\cdot)$	Light source emission function
$\Phi(\cdot)$	Sensor sensitivity function
$\Psi(\cdot)$	Joint light-sensor correlation function
$\Theta_{pf}$	Parameters of phasor field kernel: $\Omega_{pf}, \sigma_{pf}$
$\Theta_{I_s}$	Parameters of laser and sensor models: $\sigma_{I_s}, I_l, \kappa_s, \eta_s$
$\Theta_G$	Parameters of per-voxel albedo $\rho$
$\Theta$	Set of optimizing variables: $\Theta = \{\Theta_{pf}, \Theta_{I_s}, \Theta_G\}$
$\mathcal{L}$	Loss function
$\lambda_{1\dots 2}$	Loss-scale balance hyperparameters
$\Gamma$	Set of regularization terms

**Table 2: Configurations of our input datasets, including converge time and the number of iterations needed.**

	Scene	Confocal	Trans. measurement	Volume dimension	Time [hr. (#iter.)]
Synthetic	Bunny	Y	$256 \times 256 \times 1024$	$256 \times 256 \times 201$	1.93 (100)
	Dragon	Y	$256 \times 256 \times 1024$	$256 \times 256 \times 128$	1.28 (100)
	Erato	Y	$256 \times 256 \times 1024$	$256 \times 256 \times 128$	1.28 (100)
	Indonesian	Y	$256 \times 256 \times 1024$	$256 \times 256 \times 128$	1.93 (150)
Real	34	Y	$64 \times 64 \times 500$	$64 \times 64 \times 105$	1.05 (300)
	Bike	Y	$256 \times 256 \times 512$	$256 \times 256 \times 64$	1.73 (170)
	Resolution	Y	$256 \times 256 \times 512$	$256 \times 256 \times 26$	1.33 (300)
	SU	Y	$64 \times 64 \times 2048$	$64 \times 64 \times 584$	6.10 (200)
	44i	N	$130 \times 180 \times 4096$	$180 \times 180 \times 417$	3.76 (150)
	NLOS	N	$130 \times 180 \times 4096$	$180 \times 180 \times 417$	4.38 (180)